

"Abstractions and Hierarchies for Learning and Planning"

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A. Learning and Planning with Hierarchies/Abstractions:

1. Thomas L. Dean and Shieu-Hong Lin. Decomposition techniques for planning in stochastic domains. In Proceedings of the Fourteenth International Joint Conference on Artificial Intelligence (IJCAI-95), pages 1121 - 1129, 1995.

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reinforcement learning. *Discrete Event Dynamic Systems: Theory and Applications*, 13(1 - 2):41 - 77, 2003.

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18. Craig Boutilier and Richard Dearden. Approximating value trees in structured dynamic programming. In *Proceedings of the Thirteenth International Conference on Machine Learning (ICML-96)*, pages 54 - 62, 1996.

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20. Marco Wiering and Jurgen Schmidhuber. HQ-learning. *Adaptive Behavior*, 6(2):219 - 246, 1997.

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29. Carlos Guestrin and Geoffrey Gordon: Distributed Planning in Hierarchical Factored MDPs. UAI'02.
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B. Automated Hierarchy/Abstraction Discovery

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18. Bruce L. Digney: Learning hierarchical control structure for multiple tasks and changing environments. In From Animals to Animats 5: The Fifth Conference on the Simulation of Adaptive Behavior, 1998.
19. Martin Stolle and Doina Precup. Learning options in reinforcement learning. In Proceedings of the Fifth International Symposium on Abstraction, Reformulation and Approximation (SARA-02), volume 2371 of Lecture Notes in Computer Science, pages 212 - 223, 2002.
20. Vadim Bulitko, Nathan Sturtevant and Maryia Kazakevich. Speeding Up Learning in Real-time Search via Automatic State Abstraction. AAAI 2005.
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C. State Abstraction and Aggregation (some have been listed above)

(for Tom: 3, 4, 8, 11, 12, 13, 14, 15, 16, 18)

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D. Related Techniques: Factorization, Shaping, Inverse RL, Least-Squares, Off-policy learning etc.

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2. Daphne Koller and Ronald Parr. Computing factored value functions for policies in structured MDPs. In Proceedings of the Sixteenth International Joint Conference on Artificial Intelligence (IJCAI-99), pages 1332 – 1339, 1999.

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5. Andrew Y. Ng and Stuart J. Russell. Algorithms for inverse reinforcement learning. In *Proceedings of the Seventeenth International Conference on Machine Learning (ICML-00)*, pages 663 - 670, Stanford, California, 2000. Morgan Kaufmann.
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